# At the Boundaries of Syntactic Prehistory 

## Supplementary Information

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## Online Repository

The source code to replicate all the figures and the experiments presented in the paper and in the Supplementary Material is found in the following online repository (along with other relevant data and information): https://github.com/AndreaCeolin/Boundaries.

## Table S1. List of the 58 languages

The 58 languages of the dataset, along with their associated Glottolog (https://glottolog.org/glottolog/language) and ISO 639-3 codes, the family and subfamily they traditionally belong to, their location and geographic coordinates, are listed in TableS1.
The database partly differs from the one employed in Ceolin et al. (2020). Since our focus here is on macro-comparison and not on micro-variation, on the one hand we removed some varieties from the Romance, the Greek and the Finno-Ugric families which were minimally different from the other related languages of the dataset, and on the other hand we expanded the typological coverage by including two Afroasiatic (Semitic) languages (Arabic, Hebrew) and a Niger-Congo (West Atlantic) one (Wolof).

| Language | Label | Glottocode | Iso 639-3 Code | Top-level family | Family | Location | Latitude | Longitude |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Afrikaans | Afk | afri1274 | afr | Indo-European | Germanic | Cape Town | -33.91 | 18.42 |
| Arabic | Ar | stan1318 | arb | Semitic | West Semitic | Riyad | 24.71 | 46.72 |
| Archi | Arc | arch1244 | aqc | NE-Caucasian | / | Machačkala | 42.01 | 47.26 |
| Basque_Central | cB | guip1235 | eus | Basque | Guipuzcoan | Vitoria-Gasteiz | 42.85 | -2.68 |
| Basque_Western | wB | bisc1236 | eus | Basque | Biskayan | Bilbao | 43.26 | -2.93 |
| Bulgarian | Blg | bulg1262 | bul | Indo-European | Slavic | Sofia | 42.7 | 23.32 |
| Buryat | Bur | buri1258 | bua | Mongolic | Eastern Mongolic | Ulan-Ude | 51.82 | 107.61 |
| Calabrese_Northern | NCA | sout3126 | nap | Indo-European | Romance | Verbicaro | 39.75 | 15.19 |
| Cantonese | Can | cant1236 | yue | Sino-Tibetan | Sinitic | Hong Kong | 22.4 | 114.11 |
| Danish | Da | dani1285 | dan | Indo-European | Germanic | Copenhagen | 55.68 | 12.57 |
| Dutch | Du | dutc 1256 | nld | Indo-European | Germanic | Amsterdam | 52.37 | 4.89 |
| English | E | stan1293 | eng | Indo-European | Germanic | London | 51.51 | -0.13 |
| Estonian | Est | esto 1258 | ekk | Uralic | Balto-Finnic | Tallinn | 59.44 | 24.75 |
| Even_1 | Ev1 | even 1260 | eve | Tungusic | Northern Tungusic | Kustur | 67.79 | 130.4 |
| Even_2 | Ev2 | even1260 | eve | Tungusic | Northern Tungusic | Sebyan-Kyuyol | 65.29 | 130.01 |
| Evenki | Ek | even1259 | evn | Tungusic | Northwestern Tungusic | Bomnak | 54.71 | 128.86 |
| Faroese | Fa | faro1244 | fao | Indo-European | Germanic | Tórshavn | 62.01 | -6.77 |
| Finnish | Fin | finn1318 | fin | Uralic | Balto-Finnic | Helsinki | 60.17 | 24.94 |
| French | Fr | stan1290 | fra | Indo-European | Romance | Paris | 48.86 | 2.35 |
| German | D | stan1295 | deu | Indo-European | Germanic | Berlin | 52.52 | 13.4 |
| Greek | Grk | mode1248 | ell | Indo-European | Greek | Athens | 37.98 | 23.73 |
| Greek_Calabria | CG | aspr1238 | ell | Indo-European | Greek | Bova Marina | 37.93 | 15.55 |
| Greek_Cypriot | CyG | cypr1249 | ell | Indo-European | Greek | Larnaca | 34.09 | 33.62 |
| Hebrew | Heb | hebr1245 | heb | Afroasiatic | Semitic | Tel Aviv | 32.11 | 34.85 |
| Hindi | Hi | hind1269 | hin | Indo-European | Indo-Aryan | New Delhi | 28.61 | 77.21 |
| Hungarian | Hu | hung 1274 | hun | Uralic | Ugric | Budapest | 47.5 | 19.04 |
| Icelandic | Ice | icel1247 | isl | Indo-European | Germanic | Reykjavik | 64.14 | -21.94 |
| Irish | Ir | iris1253 | gle | Indo-European | Celtic | Dublin | 53.35 | -6.26 |
| Italian | It | ital1282 | ita | Indo-European | Romance | Rome | 41.9 | 12.5 |
| Japanese | Jap | nucl1643 | jpn | Japonic | / | Tokyo | 35.69 | 139.69 |
| Kazakh | Kaz | kaza1248 | kaz | Turkic | Kipchak | Almaty | 43.22 | 76.85 |
| Khanty | Kh | khan1279 | kca | Uralic | Ugric | Kazym | 63.7 | 67.24 |
| Korean | Kor | kore1280 | kor | Koreanic | 1 | Seoul | 37.57 | 126.98 |
| Kirghiz | Kyr | kirg1245 | kir | Turkic | Kipchak | Bishkek | 42.87 | 74.57 |
| Lak | Lak | lakk1252 | lbe | NE-Caucasian | / | Kumukh | 42.54 | 47.89 |
| Malagasy | Mal | plat1254 | plt | Austronesian | Malayo-Polynesian | Antananarivo | 18.88 | 47.51 |
| Mandarin | Man | mand1415 | cmn | Sino-Tibetan | Sinitic | Beijing | 39.9 | 116.41 |
| Marathi | Ma | mara1378 | mar | Indo-European | Indo-Aryan | Mumbai | 19.08 | 72.88 |
| Mari | mM | mari1278 | chm | Uralic | Volgaic | Shap | 56.44 | 47.96 |
| Norwegian | Nor | norw1258 | nor | Indo-European | Germanic | Oslo | 59.91 | 10.75 |
| Pashto | Pas | pash1269 | pus | Indo-European | Iranian | Khyber Pass | 34.09 | 71.16 |
| Polish | Po | poli1260 | pol | Indo-European | Slavic | Warsaw | 52.23 | 21.01 |
| Portuguese | Ptg | port1283 | por | Indo-European | Romance | Lisbon | 38.72 | -9.1 |
| Romanian | Rm | romal327 | ron | Indo-European | Romance | Bucharest | 44.43 | 26.1 |
| Russian | Rus | russ 1263 | rus | Indo-European | Slavic | Moscow | 55.76 | 37.62 |
| Serbo-Croatian | SC | sout1528 | hbs | Indo-European | Slavic | Zagreb | 45.82 | 15.98 |
| Siciliano | Sic | cent1963 | scn | Indo-European | Romance | Mussomeli | 37.57 | 13.75 |
| Slovenian | Slo | slov1268 | slv | Indo-European | Slavic | Ljubljana | 46.06 | 14.51 |
| Spanish | Sp | stan1288 | spa | Indo-European | Romance | Madrid | 40.42 | -3.7 |
| Tamil | Ta | tami1289 | tam | Dravidian | 1 | Madras | 13.08 | 80.27 |
| Telugu | Te | telu1262 | tel | Dravidian | / | Hyderabad | 17.39 | 78.49 |
| Turkish | Tur | nucl1301 | tur | Turkic | Oghuz | Ankara | 39.93 | 32.86 |
| Udmurt | Ud | udmu1245 | udm | Uralic | Permic | Chur | 57.07 | 53.03 |
| Uzbek | Uz | uzbe1247 | uzb | Turkic | Turkestan Turkic | Tashkent | 41.3 | 69.24 |
| Welsh | Wel | wels 1247 | cym | Indo-European | Celtic | Cardiff | 51.48 | -3.18 |
| Wolof | Wo | nucl1347 | wol | Niger-Congo | West Atlantic | Dakar | 14.69 | -17.44 |
| Yakut | Ya | yaku1245 | sah | Turkic | North Siberian Turkic | Yakutsk | 62.04 | 129.68 |
| Yukaghir | Yu | yuka1259 | yux | Yukaghir | Kolmic (Southern Yukaghir) | Kolyma | 65.5 | 151.09 |

Table S2. The dataset (attached, also available at:
https://github.com/AndreaCeolin/Boundaries/blob/main/TableS2.pdf).
TableS2 contains the 94 binary nominal parameters used for the experiments presented in the paper, set in the 58 languages of TableS1.

The table should be read as follows:
1 st column: progressive number of the parameters ( $\mathrm{p} 1, \mathrm{p} 2, \mathrm{p} 3, \ldots$ )
2nd column: acronym of the parameter
3rd column: name of the parameter
4th column: implicational constraints specifying the conditions for setting the parameter. They are expressed in a Boolean form, either as simple values of other parameters, or as conjunctions (written ','), disjunctions ('or'), or negation (‘ $\neg$ ') thereof.
All critical data used to set the parameters have been collected or checked with the help of trained native speakers, except for Irish, which has been parameterized based on specialized literature.
The list of questions used to determine the state of the parameters and instructions is available in Crisma et al (2020).
The order of the parameters is not motivated except for the ease of expression of cross-parametric dependencies (see directly below), which are organized from top-down. The alternative parameter states are encoded as ' + ' and ' - '.
The neutralizing effect of implicational dependencies across parameters is encoded as ' 0 ': the content of each parameter in such cases is entirely predictable or altogether irrelevant (the total amount of null states is 2534 out of $94 \times 58=5452$ ).
The parametric database is a refined version of that employed in Ceolin et al. (2020), with some of the parameters, their implications, and their relative order reformulated in a descriptively more accurate way.

Table S3. Table of Jaccard distances from Table S2 (attached, also available at: https://github.com/AndreaCeolin/Boundaries/blob/main/TableS3).
The matrix was derived using a Jaccard-type distance, based on the Jaccard formula described below. The comparison between the distance matrix used in this study and that used in Ceolin et al. (2020), for the overlapping languages, yields a Mantel correlation of 0.975 (see Mantel 1967). Therefore, it is expected that the exploratory analyses and the phylogenetic modeling of the distance matrix obtained from the two datasets will largely overlap. In fact, the results show just minor differences. Figures S1-S3 illustrate the major taxonomic results obtained from the distances in TableS3.

The distance measures most commonly used for two perfectly aligned binary strings of the same length are the Hamming distance (counting the number of positions where the two strings differ) and the normalized Hamming distance (obtained dividing the Hamming distance by the string length, so that all the distances are within the range [0,1]). If we use ' + ' and ' - ' as the binary symbols in the strings, as we do in this study (rather than the more usual 0 and 1 ), the formula for the latter distance is:

$$
\Delta \operatorname{Hamming}(\mathrm{A}, \mathrm{~B})=\left[\mathrm{N}_{-+}+\mathrm{N}_{+-}\right] /\left[\mathrm{N}_{-+}+\mathrm{N}_{+-}+\mathrm{N}_{++}+\mathrm{N}_{--}\right]
$$

where $\mathrm{N}_{\mathrm{XY}}$ indicates the number of positions where the string A has value X and B has value Y . When the binary strings are interpreted as indicative of the presence ('+') or absence ('-') of traits (one per position in the string), the Jaccard (or Jaccard/Tanimoto) distance encodes an additional refinement: the loci where both strings lack the trait (have a value '-') are considered irrelevant and are ignored. The formula thus removes N.. from the denominator:

$$
\Delta \operatorname{Jaccard}(\mathrm{A}, \mathrm{~B})=\left[\mathrm{N}_{-+}+\mathrm{N}_{+-}\right] /\left[\mathrm{N}_{-+}+\mathrm{N}_{+-}+\mathrm{N}_{++}\right]
$$

Note that in addition to ' $+/-$ ', syntactic characters display a third state, ' 0 ', which indicates that the parameter is redundant or irrelevant in a language. Normalised Hamming or Jaccard distances could be used to compute linguistic distances, by removing every pair involving a ' 0 ' from the computation and, crucially, considering ' $+/-$ ' as the relevant binary values. In a way, when computing distances, binary strings are shortened by getting rid of positions where ' 0 s' are present.
In Longobardi and Guardiano (2009) and Longobardi et al. (2013) a normalized Hamming distance has been used to compute linguistic distances. This choice was appropriate given that in the framework of Principles \& Parameters ' $+/-$ ' were treated as being of equal markedness status. However, recent developments have re-addressed this type of assumption. Specifically, it is agreed that certain parameter values are marked, while others can be considered as 'default' settings. In our system, one of the two opposite values of all parameters (namely '-') represents a default setting, which can be interpreted as the absence of a trait, while the other ' + ' always requires some specified empirical evidence to be set (Crisma et al. 2020). Given this asymmetry, we find a Jaccard-type metric like the one defined above, rather than a Hamming-type metric, to be more appropriate to encode syntactic distances. Therefore, adopting a Jaccard distance corresponds to making the idealization that if two languages both change a ' + ' value into a '-' value in the same parameter, this does not constitute evidence of a shared innovation; for, it only represents a resetting to the unmarked state of mental grammars. On the contrary, convergence in the opposite change (from ' - ' to ' + ') is taken as stronger evidence of shared innovation.
Consider also that Franzoi et al. (2020) have developed metric distances alternative to ours in order to capture structural dependencies among characters. Their work interestingly shows that variation in the choice of distance formulae produces limited perturbations of the robustness of the signal when applied to syntactic data.

## Figure S1. Heatmap

The distance matrix in Table S3 is visualized through the heatmap in FigureS1. The languages have been juxtaposed following the output of a hierarchical clustering algorithm, so that groups of languages sharing low distances (in blue) form squares along the diagonal.


Instructions to visualize the heatmap in the text.

1. Go to the page https://software.broadinstitute.org/morpheus/
2. Upload to the page the file jaccard_distances.txt (Table S3) and click the "OK" button to visualize the heatmap
3. In the "Tools" menu, select the option "Hierarchical clustering", and then the following options:
a. Metric $>$ Matrix values (from a precomputed distance matrix)
b. Linkage method $>$ average
c. Cluster > Rows and columns

Click the "OK" button.
4. To visualize the same color distribution as Figure 1, follow the instructions below:
a. In the "View" menu, select "Options"
b. In the "Color Scheme" window:
i. Uncheck the "Relative color scheme" choice
ii. "Maximum" $>0.778$
iii. "Add color stop"
iv. "Selected color" > yellow
v. "Selected value" $>0.426$ (the mean of the distance matrix)

Figure S2. UPGMA tree.
The tree in Figure S2 has been produced using PHYLIP
(https://evolution.genetics.washington.edu/phylip.html, Felsenstein 1989), and visualised using the Mesquite software (https://www.mesquiteproject.org, Maddison and Maddison 2018).


Figure S3. UPGMA (bootstrapped) tree.


The UPGMA tree in Figure S3 has been generated using a modified bootstrapping procedure. Bootstrapping is used to establish the robustness of the nodes, and to determine whether the internal topology of the tree is robust to resampling.
The bootstrapping technique resamples the whole dataset by selecting each character with equal probability and recreating a matrix of the same length. The content of the new matrix is different from the original matrix, because some characters might be absent and some others might be present multiple times as a consequence of the sampling procedure. This allows one to estimate the robustness of the dataset by repeating the same analysis on different samples of the dataset.
Since the Jaccard distance between two languages excludes all parameters that are set to ' 0 ' in either one of them, a standard bootstrapping procedure runs the risk of making a pair of languages not comparable, because in some replicas the number of identities plus differences can reduce to zero, and then yield a zero denominator for the Jaccard formula. For this reason, we decided to adopt a
moderated bootstrap procedure, by creating 1000 datasets in which only six parameters are resampled. Since the minimum number of comparable parameters between any two languages in the dataset is seven, a resampling of six parameters will assure that any two strings are technically comparable by means of the Jaccard distance.
The UPGMA tree presented in the text is a consensus tree resulting from applying UPGMA to the 1000 replicas of the dataset.
The bootstrapping technique is insufficient as a device to assess the robustness of clusters with our data, and this is one reason to develop the statistical testing strategy presented in the article. The divergence between the outcomes of the two procedures is evidenced in Table S2.
In Table S4, we singled out the nodes which have been tested in the article (1st column), along with the result of the statistical test ( 2 nd column) next to their bootstrapping score (3rd column).The rows of TableS4 are arranged in decreasing order of the value of the test statistic.

Table S4. The groups of languages tested in the paper and their bootstrapping scores.
In blue: clusters which test positive to our statistical procedure but receive bootstrap scores $<500$; in red: clusters which test negative to our statistical procedure but receive bootstrap scores $>500$.

| Volgaic/Permic | $\mathrm{d}=0.048$ | 999 |
| :--- | :--- | :--- |
| Tungusic/Turkic | $\mathrm{d}=0.158$ | 737 |
| Korean/Japanese | $\mathrm{d}=0.182$ | 996 |
| Germanic/Slavic | $\mathrm{d}=0.205$ | 547 |
| Tungusic-Turkic/Buryat | $\mathrm{d}=0.223$ | 653 |
| Volgaic-Permic/Balto-Finnic | $\mathrm{d}=0.225$ | 593 |
| Germanic-Slavic/Greek | $\mathrm{d}=0.244$ | 667 |
| NE Caucasian/Dravidian | $\mathrm{d}=0.263$ | 596 |
| Volgaic-Permic-Balto-Finnic/Ugric | $\mathrm{d}=0.275$ | 612 |
| Greek-Slavic-Germanic/Romance | $\mathbf{d}=\mathbf{0 . 2 7 7}$ | $\mathbf{3 4 2}$ |
| Greek-Slavic-Germanic-Romance/Indo-Iranian | $\mathbf{d}=\mathbf{0 . 2 9 6}$ | $\mathbf{3 4 2}$ |
| Balto-Finnic+Volgaic-Permic-Ugric/Tungusic-Turkic-Buryat | $\mathbf{d}=\mathbf{0 . 3 0 7}$ | $\mathbf{3 6 0}$ |
| Greek-Slavic-Germanic-Romance-Indo-Iranian/Celtic | $\mathbf{d}=\mathbf{0 . 3 2 4}$ | $\mathbf{4 1 3}$ |
| Uralo-Altaic/Yukaghir | $\mathrm{d}=\mathbf{0 . 3 4 2}$ | $\mathbf{7 9 9}$ |
| Wolof/Cantonese-Mandarin | $\mathrm{d}=\mathbf{0 . 4}$ | $\mathbf{8 6 4}$ |
| Basque/Japanese-Korean | $\mathbf{d}=\mathbf{0 . 5}$ | $\mathbf{5 1 7}$ |

It is immediately obvious that the two outcomes only partially correlate. In particular they are quite complementary in the following cases:

1) all the three nodes that include Romance display a bootstrap score below 500, though their mean distances are below the statistical threshold. This suggests that, although the significance testing algorithm clearly recognizes these groups as families because they are similar enough to each other, they also exhibit some accidental similarities with languages outside of their groups.
2) the case of Uralo-Altaic best exemplifies this case: its bootstrap value is 360 , but goes up to 799 if we include Yukaghir; however the statistical algorithm suggests that only the former group can be safely established. This depends on the fact that Yukaghir exhibits some similarities with Uralic and Altaic languages, but not outside of the group, which means that although occasionally UPGMA will place Yukaghir within either group, it would rarely place it farther than the Uralo-Altaic node. But at the same time, Altaic and Uralic are sufficiently similar to pass the test, though different enough from Yukaghir for the whole set not to test positive to it (also cf. the similar case of bootstrap values for the three Tungusic languages, among the lower nodes in Fig. S3).
3) The opposite case is exemplified by two other nodes which are remarkably above 500 but far from passing the statistical test: Basque/Japanese-Korean (517) and especially Wolof/Cantonese-Mandarin (864). The only explanation for the high bootstrap score of these groups is long-branch attraction (Bergsten 2005), because the languages exhibit internal distances higher than the overall mean of the sample ( 0.444 and 0.556 , respectively, thus insignificant from the viewpoint of the statistical test), but also much lower than with the rest of the dataset.

In conclusion, with this type and amount of characters, a statistical testing procedure such as we present in the text resists the effects of accidental similarities and random sampling of taxonomic units better than bootstraping techniques.

Table S5. Great Circle geographical distances of the languages of the sample (attached, also available at: https://github.com/AndreaCeolin/Boundaries/blob/main/TableS5).

This table contains a matrix of Great Circle Distances (in nautical miles) calculated using the coordinates in Table S1. Afrikaans was not included.

## Section S1: Generating possible languages

Since the characters we used are not independent, the probability of occurrence of each pair using the binomial coefficient cannot be calculated. The binomial formula is based on independent trials, and therefore does not account for the fact that a specific result of an event might determine the outcome of a subsequent event. Therefore, we devised a method to statistically test the probability of relatedness for larger language groups using a posterior distribution generated by a population of randomly generated strings, thereby broadly following a Bayesian framework.
Bortolussi et al. (2011) was the first attempt to elaborate a way to randomly generate admissible ternary strings of type $\{+,-, 0\}$ compatible with the implicational constraints. The naive idea to generate a string at random and discard it when it was not admissible did not work because the probability of hitting an admissible string was too low. However, some of the implication rules were simple enough to be directly built into the random generator, which thus yielded 'quasi-admissible' strings totally at random: the result was that the probability of hitting a quasi-admissible string that was also admissible became manageable.
A key property of the algorithm is that it assumes a uniform distribution of admissible languages in string selection. The hypothesis of a uniform distribution among possible languages is not unproblematic. In Table S6, for instance, languages with a ' - ' at the first parameter are selected by the algorithm with a probability of 0.25 , disregarding any information arising from the sample (for instance, the fact that they can be as frequent in the world as languages with ' + ' at P 1 ). This is because, owing to the implicational rules, out of the eight combinatorial possibilities only four different languages exist which in reality represent the entire space of variation, and therefore each one is chosen with a probability of $1 / 4$.
Therefore, a uniform distribution over languages tends to include languages bearing exceptional similarity to each other as the parameter values that activate many other parameters tend to be overrepresented with respect to those that neutralize them. This results in the production of too low a mean distance between the random language pairs.
We decided to modify the algorithm to account for all the implicational constraints in the random generator: we first set the independent parameters and created the strings incrementally, and then explored only those parameters that were compatible with the implicational structure, while automatically assigning a ' 0 ' value to the other parameters.
This strategy requires that a probability be associated to each value for each parameter. Therefore, we estimated the probabilities using the empirical distribution of the parameter values in our sample. This empirical estimate should also help us better control for biases towards certain parameter settings produced by general and external factors, to the extent they are detectable from the real-language sample. However, the 58 languages of our sample fall into 15 well-established families, therefore one can safely assume that these languages have ultimately evolved from 15 ancestors, and the probability of parametric values must be calculated considering this fact. Since such families are instantiated by an unbalanced number of languages, we took into account the cardinality of each language family in our sample, so as to enable the probabilistic information arising from each of them to be equally weighted in the generation of possible languages. We defined a 'family-ratio' as the ratio of ' + ' values for a certain parameter in the languages of a family over the total number of non-zero values. Every hypothetical language is generated with each parameter value having a ' + ' with probability equal to the arithmetic average of the family-ratios for ' + ' in that parameter within our sample. This means that, for the purposes of our algorithm, each language family is represented as an independent
observation. All the implied values are automatically assigned a ' 0 ' by the algorithm. Thus, we ensure that in the case of a sample like the one shown in Table S6, the languages are ' + ' or '-' with $p=0.5$, using the distributional information of the sample as an approximation of the space of variation (see Table S7). Note that the actual variation in our real sample is almost always different from what would be expected from the equiprobability assumption, and that each parameter might exhibit different average ratios. Our algorithm takes both facts into consideration while generating the strings.

Table S6 - The sampling algorithm of Bortolussi et al. (2011). Each language is sampled with the same probability, implying that the space of the distribution is biased towards those parameters which have a lot of dependencies. In this case, + P1 languages cover $75 \%$ of the space of variation, while P1 languages cover $25 \%$ of it.

|  | L1 | L2 | L3 | L4 | L5 | L6 | L7 | L8 |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| P1 | + | + | + | + | - | - | - | - |  |  |  |  |  |  |
| P2 (only if +P1) | + | + | - | - | 0 | 0 | 0 | 0 |  |  |  |  |  |  |
| P3 (only if +P2) | + | - | 0 | 0 | 0 | 0 | 0 | 0 |  |  |  |  |  |  |
| Probability of L_ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 2 5}$ | $\mathbf{0 . 2 5}$ |  |  |  |  |  |  |  | $\mathbf{0 . 2 5}$ |  |  |  |

Table S7-The new sampling algorithm. Languages are created with ' + ' values assigned following the average ratio. Therefore, the languages which are set on parameter values that activate several others parameters are not overweighted, and the distribution is determined by the average of the empirical values of the languages of the real sample.

|  | L1 | L2 | L3 | L4 | L5 | L6 | L7 | L8 | Average '+' ratio |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| P1 | + | + | + | + | - | - | - | - | $\mathbf{0 . 5 0}$ |  |  |  |  |  |  |
| P2 (only if +P1) | + | + | - | - | 0 | 0 | 0 | 0 | $\mathbf{0 . 5 0}$ |  |  |  |  |  |  |
| P3 (only if +P2) | + | - | 0 | 0 | 0 | 0 | 0 | 0 | $\mathbf{0 . 5 0}$ |  |  |  |  |  |  |
| Probability of L_ | $\mathbf{0 . 1 2 5}$ | $\mathbf{0 . 1 2 5}$ | $\mathbf{0 . 2 5}$ |  |  |  |  |  |  |  | $\mathbf{0 . 5 0}$ |  |  |  |  |

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